Strong gravity effects in binary systems of neutron stars and black holes: an effective action approach



Mons, December 10th, 2013

JS is supported by **FCT** (Portugal)

Outline

Motivation

- Strong gravity
- Neutron star
- Tidal forces and resonances
- 2 Effective action and strong field gravity
 - Effective theory for compact objects
 - Philosophy
 - Example: adiabatic tidal deformation
- Oynamic tidal interactions in Newtonian gravity
 - Tidal forces in Newtonian gravity
 - Effective theory point of view on tidal interactions
 - Convenient concept: response function
 - Analogy with electronics

Relativistic case

- Identification of external field and response
- Relativistic response

Outlook

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General relativity is expected to break down for strong field strengths.

Currently our best chance to test strong gravity:

compact astrophysical objects!

Black holes: clean (vacuum solutions); but observations difficult

Neutron stars (NS):

- strong gravity in NS interior (sometimes stronger than at black holes horizor)
- alternative theories can predict drastically different NS structure: oscillation modes, mass-radius relation, spontaneous scalarization

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A neutron star model

pics/neutronstar

Neutron star picture by D. Page

www.astroscu.unam.mx/neutrones/

"Lab" for various areas in physics

- magnetic field, plasma
- crust (solid state)
- superfluidity
- superconductivity
- unknown matter in core condensate of quarks, hyperons, kaons, pions, ...?

accumulation of dark matter ?

Related objects:

- pulsars
- magnetars
- quark stars

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tidal forces in inspiraling binaries \longleftrightarrow oscillation modes of neutron stars

 \Rightarrow resonances!

resonances probably relevant for short gamma-ray bursts

[Tsang et.al., PRL 108 (2012) 011102]

pics/doublepulsar

binary neutron stars

Swift/BAT, nasa.gov

mode spectrum from gravitational waves: gravito-spectroscopy

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Effective theory for compact objects

See: [Goldberger, Rothstein, PRD **73** (2006) 104029] [Goldberger, Ross, PRD **81** (2010) 124015]

Effective theory: important idea from statistical physics, quantum field theory

Starting point: An action for a "full theory" Sfull

"Integrate out" short scale (UV) part of the metric g_{UV} :

$$\expig(rac{i}{\hbar} S_{\mathsf{eff}}[g_{\mathit{IR}},\mathsf{matter}]ig) = \int Dg_{UV}\, \expig(rac{i}{\hbar} S_{\mathsf{full}}[g_{\mathit{IR}} + g_{UV},\mathsf{matter}]ig)$$

We are only interested in the classical part of the path integral.

On large scales (IR), a mass distribution looks like a point-particle:

$$S_{
m eff,matter}[g_{IR},
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 $E_{ab} \sim R_{acbd} u^c u^d, \qquad Q^{ab} \sim
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Starting point: single object, e.g., neutron star

Idea

Multipoles describe compact object on macroscopic scale

state variables $(p, V, T) \iff$ multipoles (m, S, Q)equations of state \iff effective action correlation \iff response

Approximations for binary system using effective theory:

- Effective point-particle action with dynamical multipoles
- Response functions (propagators) for multipoles

 \Rightarrow Predictions: gravitational waves, gamma-ray bursts, pulsar timing

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Example: adiabatic tidal deformation

for NS, e.g. Hinderer & Flanagan (2008); Damour, Nagar (2009); Binnington, Poisson (2009)

• Static, linear NS perturbation:

 $-Q = \mu_2 E$

- Tidal force *E* (curvature)
- Dim.-less 2nd Love number k₂:

$$k_2=\frac{3}{2}\frac{\mu_2}{R^5}$$

- Measure for grav. polarizability
- Compactness $c = \frac{Gm}{R}$
- k₂, μ₂ encode strong gravity effects in the interior
- beyond the adiabatic case:

[Bini, Damour, Faye, PRD 85 (2012) 124034]

[Maselli, Gualtieri, Pannarale, Ferrari, PRD 86 (2012) 044032]



see Damour, Nagar, PRD 80 (2009) 084035

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Simple case: linear perturbation of nonrotating barotropic stars temperature-independent equation of state see e.g. [Press, Teukolsky, ApJ **213** (1977) 183]

Displacement $\vec{\xi} :=$ perturbed – unperturbed location of fluid elements

$$\vec{\vec{\xi}} + \mathcal{D}\vec{\vec{\xi}} = (\text{external forces})$$
$$\mathcal{D}\vec{\vec{\xi}} := -\vec{\nabla} \left\{ \left[\frac{\mathcal{C}_s^2}{\rho_0} + 4\pi G \Delta^{-1} \right] \vec{\nabla} \cdot (\rho_0 \vec{\xi}) \right\}$$

 ρ_0 : unperturbed mass density

s: speed of sour

G: Newton constant

The operator \mathcal{D} :

- differential $\vec{\nabla}$ and integral Δ^{-1} operators
- linear, nonlocal, spherical symmetric
- Hermitian w.r.t. compact measure $dm_0 := \rho_0 d^3 x$

[Chandrasekhar, ApJ 139 (1964) 664–674]

⇒ Eigenfunctions of D are the normal oscillation modes of the star with discrete, real eigenvalues $\omega_{n\ell}^2 \rightarrow$ oscillation frequencies

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Effective theory point of view on tidal interactions Chakrabarti, Delsate, Steinhoff, PRD 88 (2013) 084038

Full theory: variational fluid dynamics, linear perturbation

Integrate out small scales, mode decomposition:

$$\vec{\xi} = \sum_{n\ell m} A_{n\ell m}(t) \vec{\xi}_{n\ell m}^{\text{NM}}(\vec{x})$$

Result for effective action, quadrupolar truncation $\ell = 2$:

$$S_{\text{eff,matter}} = \int dt \left[\frac{1}{2} m \dot{\vec{z}}^2 - m\Phi + \frac{1}{2} \sum_{n,m} \left[|\dot{A}_{n2m}|^2 - \omega_n^2 |A_{n2m}|^2 - I_n A_{n2m} E_{2m} \right] + \dots \right]$$
$$E_{2m} \sim E_{ab} = \partial_a \partial_b \Phi, \qquad n = \text{mode number}$$

Overlap integrals I_n : coupling constants Gravito-spectrum: ω_n and I_n

Try this with a nonlinear extension of Newtonian gravity?

Chakrabarti, Delsate, Steinhoff (IITG/UMONS/IST)

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quadrupolar response:

poles \Rightarrow resonances!

$$F = \sum_{n} \frac{I_n^2}{\omega_n^2 - \omega^2}$$

 ω_n : mode frequency I_n : overlap integral R: radius

Computation of I_n through fit of $F \Rightarrow$ generalizes to relativistic case

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Analogy with electronics



$$\frac{Q}{U} = \frac{1}{i\omega Z}$$
$$= \sum_{n} \frac{\frac{1}{L_{n}}}{\frac{1}{C_{n}L_{n}} - \omega^{2}}$$

$$\frac{Q}{E} =: F$$

$$= \sum_{n} \frac{l_{n\ell}^2}{\omega_{n\ell}^2 - \omega^2} \quad Q: \text{ quadrupole}$$

$$E: \text{ external tidal field}$$

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external quadrupolar field

Newtonian:

 $r^{\ell+1}$ relativistic, adiabatic $\omega = 0$ $r^{\ell+1} {}_2F_1(...; 2m/r)$ relativistic, generic ω :

$$X_{\rm MST}^{\ell}$$

where [Mano, Suzuki, Takasugi, PTP 96 (1996) 549]

$X_{\rm MST}^{\ell} = e^{-i\omega r} (\omega r)^{\nu} \left(1 - \frac{2m}{r}\right)^{-i2m\omega} \sum_{n=-\infty}^{\infty} \cdots \times \left[\frac{r}{2m}\right]^n {}_2F_1(\dots; 2m/r)$

Renormalized angular momentum, transcendental number: $\nu = \nu(\ell, m\omega)$



quadrupolar response





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 $r^{-\ell}$

 $r^{-\ell} _{2}F_{1}(...; 2m/r)$

$$X_{\rm MST}^{-\ell-1}$$



external quadrupolar field

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quadrupolar response



 $X_{\rm MST}^{-\ell-1}$

Identification of external field and response by considering generic ℓ (analytic continuation)

Relativistic response

Chakrabarti, Delsate, Steinhoff, arXiv:1304.2228

• Numerical neutron star perturbation matched to

$$X = A_1 X_{\rm MST}^{\ell} + A_2 X_{\rm MST}^{-\ell-}$$

- X_{MST}^{ℓ} , $X_{MST}^{-\ell-1}$ related to effective point-particle source via variation of parameters
- Point-particle source requires regularization (here: Riesz-kernel)
- Regularization introduces dependence on scale μ₀
- Fit for the response:

$$F(\omega) \approx \sum_{n} \frac{I_n^2}{\omega_n^2 - \omega^2}$$

- Just like in Newtonian case!
- Relative error less than 2%
- Relativistic overlap integrals: *I_n*
- Matching scale μ_0 is fitted, too

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Next steps:

- More realistic neutron star models: rotation, crust, ...
- Connection to gamma-ray bursts: shattering of crust

The search for universality among different NS models:

- I-Love-Q [Yagi, Yunes, Science 341 (2013) 365]
- I-Q, strong rotation [Chakrabarti, Delsate, Gürlebeck, Steinhoff, arXiv:1311.6509]
- I-Love-Q in EiBI [Sham, Lin, Leung, arXiv:1312.1011]
- quadrupole-octopole [Pappas, Apostolatos, arXiv:1311.5508]
- . . .
- are there universal relations for some overlap integrals?

Prospect in scalar-tensor theories:

- scalarization in NS [Damour, Esposito-Farese, PRL 70 (1993) 2220]
- scalarization in BH [Cardoso, Carucci, Pani, Sotiriou, PRL 111 (2013) 111101]
- floating orbits [Cardoso, Chakrabarti, Pani, Berti, Gualtieri, PRL 107 (2011) 241101]

Thank you for your attention

Chakrabarti, Delsate, Steinhoff (IITG/UMONS/IST)

Strong gravity effects in binary systems

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- are there universal relations for some overlap integrals?

Prospect in scalar-tensor theories:

- scalarization in NS [Damour, Esposito-Farese, PRL 70 (1993) 2220]
- scalarization in BH [Cardoso, Carucci, Pani, Sotiriou, PRL 111 (2013) 111101]
- floating orbits [Cardoso, Chakrabarti, Pani, Berti, Gualtieri, PRL 107 (2011) 241101]

Thank you for your attention